

## Properties of color-flavor locked strange quark matter in an external strong magnetic field\*

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The properties of color-flavor locked strange quark matter in an external strong magnetic field are investigated in a quark model with density-dependent quark masses. Parameters are determined by stability arguments. It is found that the minimum energy per baryon of the color-flavor locked (MCFL) matter decreases with increasing magnetic-field strength in a certain range, which makes MCFL matter more stable than other phases within a proper magnitude of the external magnetic field. However, if the energy of the field itself is added, the total energy per baryon will increase.

Keywords: Strange quark matter, MCFL, Mass-density-dependent model

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### I. INTRODUCTION

Strange quark matter (SQM) is an interesting topic [1] not only because of its great theoretical significance, but also its many applications, e.g., in studying quantum chromodynamics (QCD) phase diagrams [2–6], properties of strangelets [7, 8], and the structure of compact stars [9, 10], etc. In 1984, Witten conjectured that quark matter with strangeness might be the true ground state of QCD [11]. Soon after Witten's conjecture, Farhi and Jaffe studied the stability of SQM with the conventional MIT bag model and found that SQM is absolutely stable around the normal nuclear density for a wide range of model parameters [12]. Since then, SQM has become a main topic in a number of meaningful works [13–20].

It has been demonstrated that SQM at high density may be in the color-flavor locked (CFL) phase where quarks with different color and flavor quantum numbers form Cooper pairs with a large binding energy [21]. It is, thus, possible that CFL matter, rather than nuclear matter, may be the ground state of strange quark matter at high density. Therefore, a compact star is suggested to include color superconducting quark matter in its inner core [22].

It is generally believed that properties of quark matter have been strongly affected in the presence of a strong magnetic field [23, 24]. A strong magnetic field widely exists on the surface of stars. The observed magnetic field strength on the surface of pulsars could be in the order of  $10^{12}$ – $10^{13}$  G. And the magnetic-field strength on the so-called magnetars could be in the order of  $10^{14}$ – $10^{15}$  G or even higher [25, 26]. In fact, the biggest magnetic field that can be sustained by strange stars was estimated to be as large as  $1.5 \times 10^{20}$  G [27]. Although the origin of the strong magnetic field is not completely clear and still under active investiga-

tions, some ways to understand its existence are available, e.g., the amplification of the relatively small magnetic field during the star's collapse with magnetic flux conservation [28], and the magneto-hydrodynamic dynamo mechanism with large magnetic fields generated by rotating the plasma of a proton-neutron star [29]. Furthermore, noncentral high-energy heavy-ion collisions could generate intense magnetic fields as high as about  $10^{19}$  G [27], corresponding to  $eB_m \sim 6m_\pi^2$ , where  $e$  is the fundamental electric charge and  $m_\pi$  is the pion mass. It is therefore necessary to study the properties of CFL in the presence of an external magnetic field.

In past years, magnetized strange quark matter (MSQM) and CFL matter have been studied with many phenomenological models, e.g., the bag model [30], the Nambu-Jona-Lasinio (NJL) model [31–36], and the mass-density dependent model [37, 38], etc. The MCFL matter has a wide range of model parameters characterized by the so-called stability window [39], and has also been studied in the NJL model [40–44], as well as in the quasiparticle model [45, 46].

As is well known, particle masses vary with environment, i.e., they depend on density or chemical potential. The equiv-particle model [1, 2] takes this effect into account by density-dependent quark masses. In recent years, this model has been extensively applied to study the properties of SQM [1, 15, 47–55]. In this paper, we extend it to investigate the properties of CFL matter when a strong magnetic field appears. It is found that MCFL matter is more stable than the other phases within a proper magnitude of the magnetic field. At a fixed density, the energy density of MCFL matter varies with the magnetic field strength. At  $B_m \geq 10^{19}$  G, the energy per baryon, pressure, and quark chemical potentials get smaller because the quantum number of the corresponding Fermi momentum approaches to zero.

This paper is organized as follows. In Section II, we give the thermodynamic formulas used for the study of MCFL matter in the equiv-particle model with density-dependent quark masses. Then we present the numerical results and discussions in Section III. Section IV is a short summary.

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## II. THERMODYNAMIC TREATMENT

Our starting point is the thermodynamic potential density of a free-particle system, i.e.

$$\Omega_f = \sum_i \frac{2g_i}{(2\pi)^3} \int \left( \sqrt{p^2 + m_i^2} - \mu_i \right) d^3p, \quad (1)$$

where the summation index,  $i$ , goes over  $u, d, s$  quarks and electrons,  $m_i$  is the corresponding particle mass,  $\mu_i$  is the chemical potential,  $g_i$  is the degeneracy factor with a value of 3 for quarks and 1 for electrons, while the degeneracy due to spin has been denoted by a factor of 2.

In the case of CFL phase, due to the energy gap,  $\Delta$ , determined by solving the gap equation, a new term should be added to the above expression. The thermodynamic potential density of CFL matter is then

$$\Omega_{\text{CFL}} = \sum_i \frac{2g_i}{(2\pi)^3} \int (\varepsilon_i - \mu_i) d^3p - \frac{3\Delta^2 \bar{\mu}^2}{\pi^2} + B, \quad (2)$$

where  $\varepsilon_i = \sqrt{p^2 + m_i^2}$  is the dispersion relation of a free particle with a mass of  $m_i$ ,  $\bar{\mu} = (\mu_u + \mu_d + \mu_s)/3$  is the average of the quark chemical potentials. The second term is from the pairing contribution, and the last term,  $B$ , is the famous MIT bag constant to take the vacuum energy into account.

To consider the effect of a magnetic field, we assume a constant magnetic field with a strength of  $B_m$  along the  $z$  axis. Due to Landau diamagnetism, the single particle energy spectrum can be written as

$$\varepsilon_{i,l} = \sqrt{p_z^2 + m_i^2 + 2|q_i|B_m[l + 1/2 - \text{sgn}(q_i)S]}, \quad (3)$$

where  $p_z$  is a component of the particle momentum along the direction of the magnetic field,  $q_i$  is the electric charge of quarks when  $q_u = 1/3$ ,  $q_d = q_s = -1/3$ ,  $q_e = -1$ ,  $l = 0, 1, 2, \dots$  is the principal quantum number for the allowed Landau levels, and  $S = \pm 1/2$  refers to spin-up and spin-down states, respectively. The sign function 'sgn' equals 1 with a positive argument and  $-1$  with a negative argument.

For the sake of convenience, one normally sets  $\nu = l + 1/2 - \text{sgn}(q_i)S$ , where  $\nu = 0, 1, 2, \dots$ . The single particle energy becomes

$$\varepsilon_{i,\nu} = \sqrt{p_z^2 + M_{i,\nu}^2}, \quad (4)$$

where  $M_{i,\nu} \equiv \sqrt{m_i^2 + 2\nu|q_i|B_m}$ .

The integration over the  $p_x$ - $p_y$  plane in the momentum space should be replaced by

$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} dp_x dp_y \longrightarrow 2\pi |q_i| B_m \sum_{\nu} (2 - \delta_{\nu 0}). \quad (5)$$

After this substitution, Eq. (2) becomes

$$\Omega_{\text{MCFL}} = \sum_i \sum_{\nu=0}^{\nu_{\text{max}}} \frac{f_{i,\nu}}{2} \int_0^{p_{i,\nu}} (\varepsilon_{i,\nu} - \mu_i) dp_z - \frac{3\Delta^2 \bar{\mu}^2}{\pi^2} + B, \quad (6)$$

where we have used the notations:

$$p_{i,\nu} \equiv \sqrt{\mu_i^2 - M_{i,\nu}^2}, \quad f_{i,\nu} \equiv \frac{g_i |q_i| B_m}{4\pi^2} (2 - \delta_{\nu 0}). \quad (7)$$

The upper bound  $\nu_{\text{max}}$  of the summation index  $\nu$  in Eq. (6) is

$$\nu_{\text{max}} \equiv \text{int} \left( \frac{\mu_i^2 - m_i^2}{2|q_i|B_m} \right), \quad (8)$$

where the function  $\text{int}(x)$  means taking the integer part of its argument  $x$ .

After carrying out the integration in Eq. (6), we have the thermodynamic potential density in the conventional bag model

$$\Omega_{\text{MCFL}} = - \sum_i \sum_{\nu=0}^{\nu_{\text{max}}} f_{i,\nu} \left[ \mu_i \sqrt{\mu_i^2 - M_{i,\nu}^2} - M_{i,\nu}^2 \text{arcsch} \left( \frac{\mu_i}{M_{i,\nu}} \right) \right] - \frac{3\Delta^2 \bar{\mu}^2}{\pi^2} + B. \quad (9)$$

To include medium effect, the quark masses should be density/chemical potential dependent. In the chemical potential dependent case, one can use the quasiparticle model, as has been done in Ref. [45]. In the density-dependent case, the actual chemical potential,  $\mu_i$ , should be replaced with an effective chemical potential,  $\mu_i^*$  [1], i.e.

$$\Omega_0 = \sum_i \Omega_i - \frac{3\Delta^2 \bar{\mu}^2}{\pi^2} + B, \quad (10)$$

where  $\bar{\mu}$  is now understood as the average of the effective chemical potentials, and  $\Omega_i$  is connected to the effective chemical potentials by

$$\Omega_i = - \sum_{\nu=0}^{\nu_{\text{max}}} f_{i,\nu} \left[ \mu_i^* \sqrt{\mu_i^{*2} - M_{i,\nu}^2} - M_{i,\nu}^2 \text{arcsch} \left( \frac{\mu_i^*}{M_{i,\nu}} \right) \right]. \quad (11)$$

All other thermodynamic quantities can be derived from  $\Omega_0$ . Specially, the particle number density is given by  $n_i = -\partial \Omega_0 / \partial \mu_i^*$ , giving

$$n_i = \frac{g_i |q_i| B_m}{2\pi^2} \sum_{\nu=0}^{\nu_{\text{max}}} (2 - \delta_{\nu 0}) \sqrt{\mu_i^{*2} - M_{i,\nu}^2} + \frac{2\Delta^2 \bar{\mu}}{\pi^2}. \quad (12)$$

The energy density for the MCFL matter is then

$$E_{\text{MCFL}} = \Omega_0 + \sum_i \mu_i^* n_i. \quad (13)$$

Upon application of Eqs. (10)–(12), we have

$$E_{\text{MCFL}} = \sum_i \frac{g_i |q_i| B_m}{4\pi^2} \sum_{\nu=0}^{\nu_{\text{max}}} (2 - \delta_{\nu 0}) \left[ \mu_i^* \sqrt{\mu_i^{*2} - M_{i,\nu}^2} + M_{i,\nu}^2 \text{arcsch} \left( \frac{\mu_i^*}{M_{i,\nu}} \right) \right] - \frac{3\Delta^2 \bar{\mu}^2}{\pi^2} + B. \quad (14)$$

Because the quark masses are density dependent, the actual chemical potential is generally not equal to its effective one. In fact, they are linked by

$$\mu_i = \mu_i^* + \mu_I, \quad (15)$$

where  $\mu_I$  is due to the density dependence of the quark masses. Its explicit expression is obtained by applying the fundamental differential equality  $dE_{\text{MCFL}} = \sum_i \mu_i dn_i$  with Eqs. (10)–(15), giving

$$\mu_I = \sum_j \frac{\partial \Omega_0}{\partial m_j} \frac{dm_j}{dn_i}, \quad (16)$$

$$= - \sum_{j,\nu} \frac{g_j |q_j| B_m D}{18\pi^2 n^{4/3}} (2 - \delta_{\nu 0}) m_j \text{arcsinh} \left( \frac{\mu_j^*}{M_{j,\nu}} \right). \quad (17)$$

Because electrons do not participate in strong interactions, their actual chemical potential is equal to the effective one, i.e.,  $\mu_e = \mu_e^*$ .

Due to the external magnetic field, the longitudinal pressure and transverse pressure become different, i.e.

$$P_{\parallel} = -\Omega_0 + \sum_i \mu_I n_i \quad (18)$$

and

$$P_{\perp} = -\Omega_0 + \sum_i \mu_I n_i - M_f B_m, \quad (19)$$

where  $P_{\parallel}$  is the total parallel pressure and  $P_{\perp}$  is the transverse pressure. The system magnetization is given by

$$M_f = - \frac{\partial \Omega_0}{\partial B_m} = - \sum_i \left( \frac{\Omega_i}{B_m} + \frac{\partial \Omega_i}{\partial M_{i,\nu}} \frac{dM_{i,\nu}}{dB_m} \right). \quad (20)$$

Upon application of Eqs. (10), (11), and (20), we have the following explicit expressions

$$P_{\parallel} = - \sum_i \frac{g_i |q_i| B_m}{4\pi^2} \sum_{\nu=0}^{\nu_{\max}} (2 - \delta_{\nu 0}) \times \left[ -\mu_i^* \sqrt{\mu_i^{*2} - M_{i,\nu}^2} + \left( M_{i,\nu}^2 + \frac{2}{3} \frac{D}{n^{1/3}} m_i \right) \times \ln \frac{\sqrt{\mu_i^{*2} - M_{i,\nu}^2} + \mu_i^*}{M_{i,\nu}} \right] + \frac{3\Delta^2 \bar{\mu}^2}{\pi^2} - B, \quad (21)$$

and

$$P_{\perp} = \sum_i \frac{g_i |q_i| B_m}{4\pi^2} \sum_{\nu=0}^{\nu_{\max}} (2 - \delta_{\nu 0}) \times \left( -\frac{2}{3} \frac{D}{n^{1/3}} m_i + 2 |q_i| \nu B_m \right) \ln \frac{\sqrt{\mu_i^{*2} - M_{i,\nu}^2} + \mu_i^*}{M_{i,\nu}} + \frac{3\Delta^2 \bar{\mu}^2}{\pi^2} - B. \quad (22)$$

### III. THE PROPERTIES OF MCFL MATTER

In the equiv-particle model, the quark mass can be divided into two parts as

$$m_i = m_{i0} + m_I, \quad (23)$$

where  $m_{i0}$  is the quark's current mass, and  $m_I$  represents the effect due to the interaction between quarks. In principle, the density dependence of  $m_I$  should be determined from QCD. As mentioned before, however, there is no way to exactly solve QCD presently. Therefore, the density dependence is normally given phenomenologically. It can be shown that the following parametrization is reasonable,

$$m_i = m_{i0} + \frac{D}{n^{1/3}}, \quad (24)$$

where  $D$  is a fixed constant determined by stability argument,  $n$  is the total baryon number density, and the exponent of the baryon number density was derived based on the in-medium chiral condensates and linear confinement at zero temperature. Such a form satisfies  $\lim_{n \rightarrow 0} m_I = \infty$  and  $\lim_{n \rightarrow \infty} m_I = 0$ , which are the requirements of quark confinement and asymptotic freedom.

Because weak equilibrium is always reached in SQM, relevant chemical potentials satisfy

$$\mu_d = \mu_s, \quad (25)$$

and

$$\mu_u + \mu_e = \mu_s. \quad (26)$$

Therefore, the effective chemical potentials also meet the corresponding relations

$$\mu_u^* + \mu_e = \mu_d^*, \quad (27)$$

and

$$\mu_d^* = \mu_s^*. \quad (28)$$

We also have the baryon number density

$$n = \frac{1}{3} (n_u + n_d + n_s), \quad (29)$$

and the charge density

$$Q = \frac{2}{3} n_u - \frac{1}{3} n_d - \frac{1}{3} n_s - n_e. \quad (30)$$

The charge-neutrality condition requires  $Q = 0$ .

For a given total baryon number density of  $n$ , we can obtain the respective  $\mu_u^*$ ,  $\mu_d^*$ ,  $\mu_s^*$ , and  $\mu_e$  by solving Eqs. (27)–(30) with the help of Eq. (12). The number densities  $n_u$ ,  $n_d$ ,  $n_s$ , and  $n_e$  can then be obtained. The energy density is calculated by Eq. (14), while the pressures are, respectively, obtained from Eqs. (21) and (22) for different values of  $B$ ,  $D$ , and  $B_m$ .

In Fig. 1, we give the energy per baryon of SQM, MSQM, CFL matter, and MCFL matter, respectively, as a function of

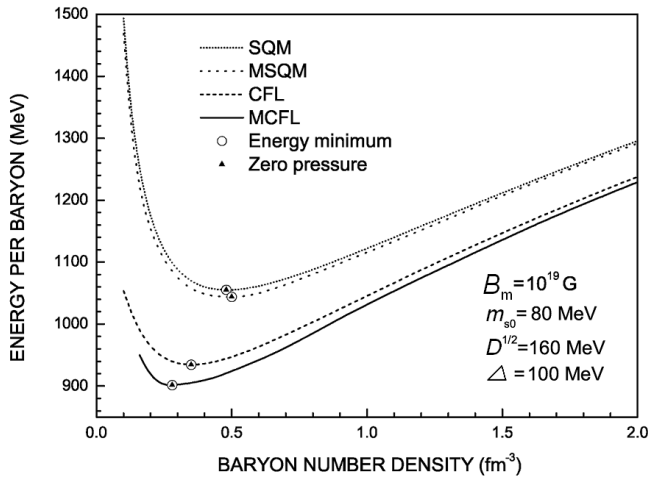


Fig. 1. Comparison of the energy per baryon versus the baryon number density for SQM, MSQM, CFL matter, and MCFL matter, respectively. The pressure at the energy minimum is exactly zero for each quark matter phase.

the baryon number density. Because the current mass of  $u/d$  quarks are very small, we simply take  $m_{u0} = m_{d0} = 0$ . But for the current mass of the strange quark, we take  $m_{s0} = 80$  MeV. The electron does not participate in the strong interaction, its mass is very tiny, and also ignored. For convenience of comparison with previous works, we take the pairing parameter to be  $\Delta = 100$  MeV. The bag constant,  $B$ , and the confinement parameter,  $D$ , are taken to be  $B^{1/4} = 140$  MeV and  $D^{1/2} = 120$  MeV. In our calculation, we assume the magnetic field to be constant with its direction along the  $z$  axis. Because the system will become unstable when the magnetic field strength is higher than  $10^{20}$  G, as discussed by Chakrabarty [23], we take the magnetic field strength to be  $B_m = 10^{19}$  G. From top to bottom in Fig. 1, there are three features. Firstly, the energy minimum (the solid triangle) corresponds exactly to the zero pressure (open circle) for each case. In fact, the exact coincidence of the lowest energy state and zero pressure is a basic requirement of the fundamental thermodynamics, as pointed out in Ref. [15], and derived in detail in Ref. [1]. Secondly, the energy per baryon of CFL matter and MCFL matter is lower than that of SQM and MSQM. So we can see that the quark pairing effect greatly increases the stability chances of SQM. Thirdly, the energy per baryon of MSQM and MCFL matter is lower than that of SQM and CFL matter, respectively. We can see that the external magnetic field in a proper magnitude lowers the energy per baryon through the rearrangement of the Landau energy level of magnetized quark matter. Generally, we have the inequality relation of the energy per baryon as

$$\left. \frac{E}{n} \right|_{\text{MCFL}} < \left. \frac{E}{n} \right|_{\text{CFL}} < \left. \frac{E}{n} \right|_{\text{MSQM}} < \left. \frac{E}{n} \right|_{\text{SQM}}. \quad (31)$$

In Fig. 2, we give the minimum energy per baryon of MCFL phase as a function of the magnetic field strength. When the magnetic field strength,  $B_m$ , is small, it is obvious that the energy is nearly constant. The energy per baryon

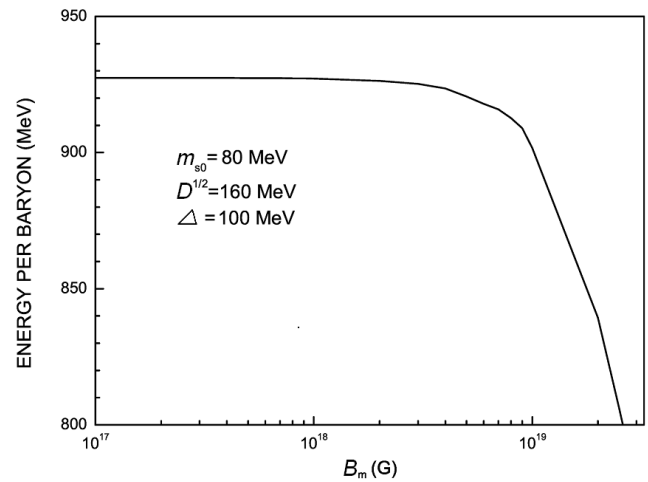


Fig. 2. The minimum energy per baryon of MCFL matter as a function of the magnetic field strength. Relevant parameters are indicated in the figure.

starts to decrease obviously as a function of the magnetic field between  $10^{18}$  G and  $10^{19}$  G. When the magnetic field strength exceeds  $10^{19}$  G, the energy per baryon decreases quickly. Therefore, an external magnetic field with proper strength lowers the energy per baryon. In this regard, one should note that the energy from the external magnetic field was not added. Otherwise, the total energy per baryon will increase.

There are different views on whether or not the energy contribution from the magnetic field should be included. If one would like to include the field contribution, one should know how the quark matter produce the magnetic field. As mentioned in the introduction, the origin of the the strong magnetic field is presently not very clear, although some ways to understand it are available. Therefore, we treat the magnetic field as an externally forced field.

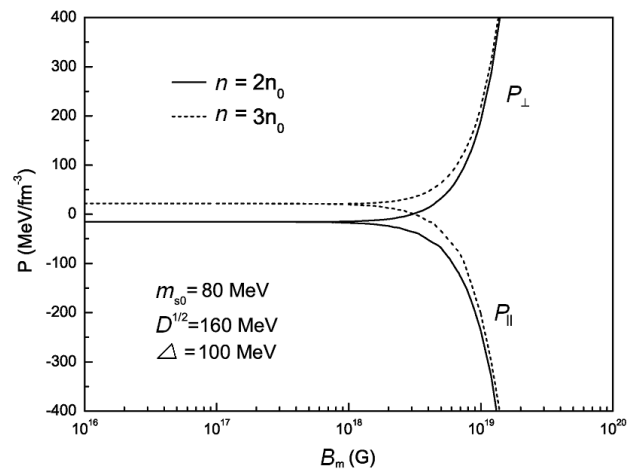


Fig. 3. The pressure in MCFL matter as a function of the magnetic field strength at two (the solid line) and three (the short-dot line) times the nuclear saturation density  $n_0 = 0.165 \text{ fm}^{-3}$ .

As is well known, the space becomes anisotropic when an external magnetic field is presented. To compare the magnitude of the longitudinal and transverse pressures, we plot, in Fig. 3, the  $P_{\parallel}$  and  $P_{\perp}$  at the given densities of  $n = 2n_0$  (the solid line) and  $n = 3n_0$  (the short-dot line) where  $n_0 = 0.165 \text{ fm}^{-3}$  is the nuclear saturation density, as functions of the magnetic field strength. The difference between  $P_{\parallel}$  and  $P_{\perp}$  reflects the breaking of the rotational symmetry by the magnetic field. We can see that the pressure stays as constant when the magnetic field strength is lower than  $10^{18} \text{ G}$ . When the magnetic field strength is larger than  $10^{18} \text{ G}$ , the pressure anisotropy starts to become noticeable: the parallel pressure,  $P_{\parallel}$ , increases far beyond the constant value, while the vertical pressure,  $P_{\perp}$ , decrease from the constant value.

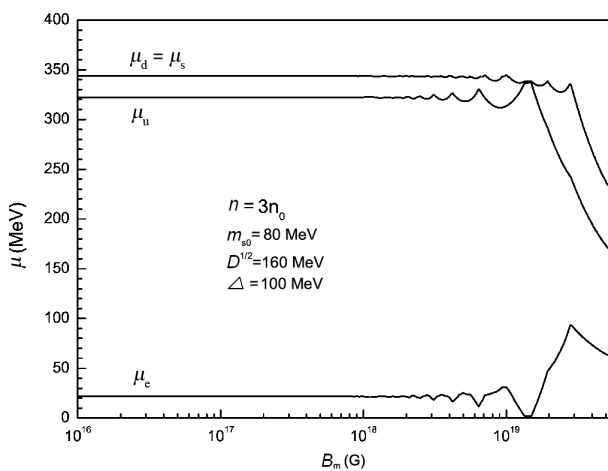


Fig. 4. The chemical potential of quarks in MCFL matter as a function of the magnetic field strength for  $n = 3n_0$ .

In Fig. 4, the chemical potentials are shown as functions of the magnetic field strength for  $n = 3n_0$ . When the magnetic

field strength,  $B_m$ , is small, all the chemical potentials,  $\mu_u$ ,  $\mu_d$ ,  $\mu_s$ , and  $\mu_c$ , are approximately constant. The chemical potentials oscillate when the magnetic field strength is in the range of  $10^{18} \text{ G}$  to  $10^{19} \text{ G}$ . When the magnetic field strength exceeds a critical value, about  $10^{19} \text{ G}$ , the energy decreases fast. At the range of  $B_m \geq 10^{19} \text{ G}$ , the chemical potentials decrease with the magnetic field. This is also the reason why the pressure oscillates and decreases when increasing the magnetic field.

#### IV. CONCLUSION

We have extended the equiv-particle model with density-dependent quark masses to the investigation of MCFL matter in an external strong magnetic field. The exact zero pressure at the energy minimum demonstrates the self-consistency of our treatment. The stability property of MCFL matter is calculated and compared with SQM, MSQM, and CFL matter. For a proper magnitude of the external magnetic field, the MCFL phase is more stable than the other phases of quark matter. The impact of the external strong magnetic field on the properties of MCFL matter is changed by the magnetic-field strength. When  $B_m \leq 10^{18} \text{ G}$ , the magnetic field affects the properties of the system only slightly. When  $10^{18} \text{ G} \leq B_m \leq 10^{19} \text{ G}$ , Landau oscillation appears in the chemical potentials, and the effect becomes obvious. When  $B_m \geq 10^{19} \text{ G}$ , the maximum Landau level  $\nu_{\text{max}}$  only takes the lowest value, and accordingly, the effects on the chemical potential, energy density, pressure are all dramatically large. Importantly in this case, the minimum energy per baryon gets smaller.

Naturally, the present study is limited in many aspects while the quark matter field is rapidly developing [56]. Therefore, further investigations are needed.

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